

Name: _____ Date: _____

Corresponding Parts of Congruent Triangles are Congruent

- When two triangles are congruent all corresponding parts* of the two triangles are also congruent.

*Corresponding parts include the angles and sides from one triangle (the pre-image) to the next (the image).

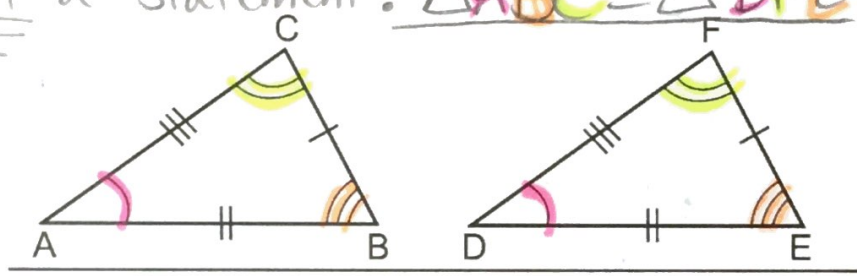
- A congruence statement matches the congruent parts in the two figures by naming them in a specific order.

Example:

Statement: $\triangle ABC \cong \triangle DEF$

Not a statement: $\triangle ABC \cong \triangle DFE$

*this would not be the correct way to name these two triangles as congruent.



Steps for Writing Your Congruence Statements for Triangles

1: Write a congruence statement for the two triangles, making sure to match up the corresponding parts.

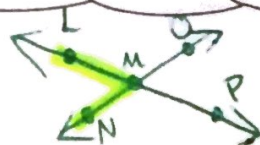
2: Use the congruence statement you just wrote to list the pairs of congruent angles.

3: Use the same congruence statement from step 1 to list the pairs of congruent sides.

* make sure to use the proper notation!

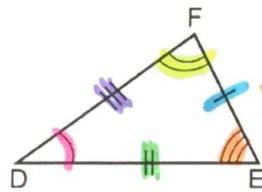
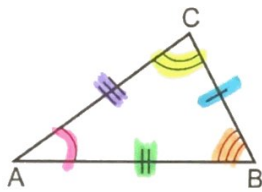
Sometimes you will need to use 3 letters to name an angle if two angles have the same vertex!

ex.



can't call it $\angle M$! Must be specific! Which M? use $\angle LMN$

Example one: Use the following triangles to write a congruence statement and name the congruent parts.



Congruence Statement: $\triangle ABC \cong \triangle DEF$

Angles

Sides

* $\angle A \cong \angle D$

* $\overline{AB} \cong \overline{DE}$

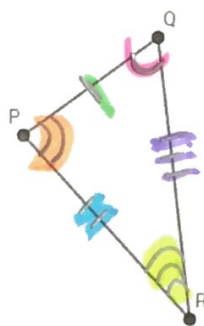
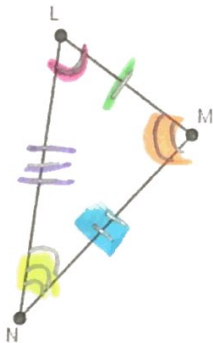
* $\angle B \cong \angle E$

* $\overline{BC} \cong \overline{EF}$

* $\angle C \cong \angle F$

* $\overline{CA} \cong \overline{FD}$

Example two: Use the angles and sides to mark the given triangle and write a congruence statement for the two triangles.



Congruence Statement: $\triangle LMN \cong \triangle PQR$

Angles

Sides

* $\angle L \cong \angle Q$

* $\overline{LM} \cong \overline{QP}$

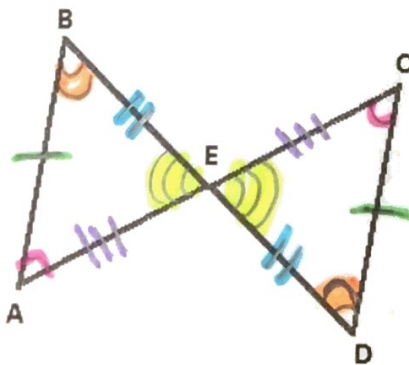
* $\angle M \cong \angle P$

* $\overline{MN} \cong \overline{PR}$

* $\angle N \cong \angle R$

* $\overline{NL} \cong \overline{RQ}$

Example three: Use the congruence statement to list all congruent sides and angles. Mark the given triangles as well.



Congruence Statement: $\triangle ABE \cong \triangle CDE$

Angles

Sides

* $\angle A \cong \angle C$

* $\overline{AB} \cong \overline{CD}$

* $\angle B \cong \angle D$

* $\overline{BE} \cong \overline{DE}$

* $\angle AEB \cong \angle CED$

* $\overline{EA} \cong \overline{EC}$

can't just call them $\angle E$ because two angles work here!

Corresponding Parts of Congruent Triangles are Congruent Theorem

(CPCTC)

- **CPCTC Theorem:** If two triangles are congruent, then corresponding sides are congruent and corresponding angles are congruent.
- **CONVERSE:** IF six pairs of corresponding sides and corresponding angles are congruent, THEN you can conclude that the two triangles are congruent.

Example:

use congruence to copy parts over to other Δ !! 😊

$\Delta RST \cong \Delta UVW$. Find all missing sides and angles.

Triangle RST

Right angle at R

Angle S = 67°

Side SR = 6 m

Hypotenuse ST = 15.6 m

Angle T = 23°

Side RT = 14.4 m

$$\begin{array}{r} 180 \\ - 90 \\ \hline 90 \\ - 67 \\ \hline 23 \end{array}$$

Triangle UVW

Right angle at U

Angle V = 67°

Side UV = 6 m

Hypotenuse VW = 15.6 m

Angle W = 23°

Side UW = 14.4 m